Fractons, dipole symmetry breaking and gravity

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In a nutshell



- Challenge longstanding beliefs in QFT (UV/IR mixing).
- Construction of quantum field theories with dipole symmetry.
- Coupling to curved background geometries.
- Spontaneous breaking of coordinate dependent symmetries.
- Connections of fractons and gravity.

Realization of dipole symmetry

Dipole symmetry \rightarrow **immobility** constraints: $\omega^2=0$.

The current conservation equation:

Coupling to A_0 and A^{ij} (symmetric),

$$S = \int d^{d+1}x \left(A_0 \rho + A_{ij} J^{ij} \right)$$
 [Pretko '16]

with gauge transformations

$$\delta A_0 = -\partial_0 \lambda_0, \quad \delta A_{ij} = \partial_i \partial_j \lambda_0$$

Realization of dipole symmetry

Linear realization of dipole symmetry for scalar ϕ :

$$\phi \to e^{i(\lambda_0 + \overline{\lambda_1} \cdot \overline{x})} \phi \longrightarrow \mathscr{L} = |\partial_0 \phi|^2 + |\partial_i \phi|^2 - g |\phi \partial_i \partial_j \phi - \partial_i \phi \partial_j \phi|^2 + \dots$$
[Pretko '18]

Gauging the monopole $\lambda_0 \rightarrow \lambda_0(t, x)$,

$$\phi \partial_i \partial_j \phi - \partial_i \phi \partial_j \phi \to e^{2i\lambda_0} \left(\phi \partial_i \partial_j \phi - \partial_i \phi \partial_j \phi + (i\partial_i \partial_j \lambda_0) \phi^2 \right)$$

We need to introduce A_{ij} such that

$$A_{ij} \rightarrow A_{ij} + \partial_i \partial_j \lambda_0, \qquad \phi \partial_i \partial_j \phi - \partial_i \phi \partial_j \phi - i A_{ij} \phi^2$$

Problems when coupling to curved background geometries, due to not gauge invariant terms!

The tool

MDMA:
$$i[P_i, Q_1^j] = \delta_i^j Q_0$$
.

[K. T. Grosvenor, C. Hoyos, F. Peña Benítez, and P. Surówka '21]

Generators: translations P_i , monopole charge Q_0 and dipole charge Q_{i_1} .

Consequences

• Construct an "ordinary" covariant derivative D_{μ} .

Ordinary vector gauge fields

- No obstruction to introducing quadratic derivative terms in the action.
- Couple to generic curved background geometries.

Dipole symmetry breaking

Having D_{μ} ,

$$\mathscr{L} = \sum_{n} |D_{\mu}\phi_{n}|^{2} + V(\phi_{n}^{\dagger}\phi_{n}).$$

By means of standard techniques, e.o.m. with dipole symmetry breaking.

The NG mode

$$\mathscr{L}_{NG}^{1-loop} = \frac{V_x^2}{240\pi \tilde{m}_{\phi}^4} \left(10\tilde{m}_{\phi}^2(\partial_t\theta)^2 - (\partial_x\partial_t\theta)^2 + (\partial_t^2\theta)^2 \right).$$

With emergent subsystem symmetry:

 $\theta(t, x) \to \theta(t, x) + f(x)$.

Moreover:

$$\omega^2 = 0.$$

Fractonic NG mode!

Results and open questions

Spontaneous dipole symmetry breaking with or without concomitant monopole breaking \rightarrow fractonic NG.

[CHMW, Goldstone physics, hydrodynamics, gravity...]

Dipole-conserving models with bosonic and fermionic matter.

Couple the model to **dynamical gauge fields** for the monopole and dipole symmetries.

Extend the analysis to **higher dimensions**.

Thank you for your attention!