Scale-separated Flux Vacua in 3D

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String Theory

- We want a single theory that explains everything: **gravity** and **quantum** physics the **very big** and the **very small**.
- String theory is the most promising candidate.
- Strings need 10 (or 11) dimensions to work!
- We don't see these extra dimensions... so where are they?

String Theory

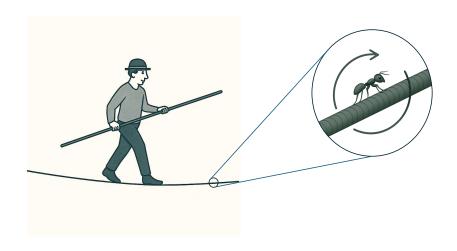
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THEY ARE COMPACTIFIED!

Compact dimensions

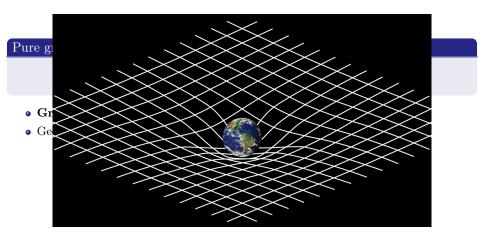


Compact dimensions



$$S_E = \int d^5 x \sqrt{-\hat{g}} \,\hat{R}$$

- ullet Gravity \longleftrightarrow Spacetime curvature
- Geometry encoded in the **metric**



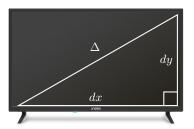
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$$\Delta^2 = dx^2 + dy^2 = \begin{pmatrix} dx & dy \end{pmatrix} \underbrace{\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}}_{q} \begin{pmatrix} dx \\ dy \end{pmatrix}$$

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$$\Delta^{2} = (d\theta \quad d\varphi) \underbrace{\begin{pmatrix} R^{2} & 0 \\ 0 & R^{2} \sin^{2} \theta \end{pmatrix}}_{q} \begin{pmatrix} d\theta \\ d\varphi \end{pmatrix}$$

$$S_E = \int d^5 x \sqrt{-\hat{g}} \,\hat{R}$$

- $\bullet \ \, \mathbf{Gravity} \longleftrightarrow \mathbf{Spacetime} \ \, \mathbf{curvature}$
- Geometry encoded in the **metric**



$$\Delta^{2} = \begin{pmatrix} dx & dy \end{pmatrix} \underbrace{\begin{pmatrix} g_{xx} & g_{xy} \\ g_{xy} & g_{yy} \end{pmatrix}}_{q} \begin{pmatrix} dx \\ dy \end{pmatrix}$$

$$S_E = \int d^5 x \sqrt{-\hat{g}} \,\hat{R}$$

$$g_5 = \left(\begin{array}{c|c} g_4 & v \\ \hline v & \phi \end{array}\right)$$

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5D metric:
$$g_{5} = \begin{pmatrix} g_{4} & v \\ \hline v & \phi \end{pmatrix}$$

$$\downarrow$$

$$S_{4D} = \int d^{4}x \sqrt{-g_{4}} \left(R - \frac{1}{4}e^{-\sqrt{3}\phi} |\mathcal{F}|^{2} - \frac{1}{2}(\partial\phi)^{2} \right)$$

$$Gravity + Maxwell + Scalar$$

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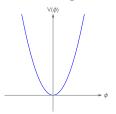
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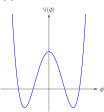
$$Gravity + \text{Maxwell} + \text{Scalar}$$

- \bullet ϕ parametrises the size of the extra dimension
- ullet Needs to be small compared with external spacetime \bullet Scale separation.

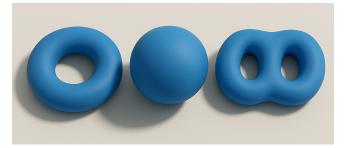
Scalar potential

• We need a scalar potential to stabilise the scalar(s)





• Different internal geometries and/or background fluxes



Set-up



- Family of 3D theories coming from type IIB string theory
- Characterised by a scalar potential with
 - 13 parameters (Fluxes)
 - 8 scalars (sizes of internal space) appearing at high powers
- Can we find a 3D theory (flux choice) allowing for scale separation?

Finding minima of scalar potential

Algebraic geometry

We don't have time for the details...

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- We found 15 independent families of vacua
- 2 of them feature parametric scale separation!!!

Thanks!